

# Quantitative Methods in Sociolinguistics

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[www.danielezrajohnson.com/sss5.pdf](http://www.danielezrajohnson.com/sss5.pdf)

## “the old testament”

There were (quantitative) (sociolinguistic) studies of language variation before Labov:

Terracher 1914.

Duraffour 1927.

Martinet 1945.

Putnam & O’Hern 1955.

Malkiel, Yakov. 1984. Revisionist dialectology and mainstream linguistics. *Language in Society* 13: 29-66.

Joseph, John E. 2002.

Koerner, E. F. K. 2003.

# “John The Baptist”

**Table I. Number of children favoring *-ing* and *-in* variant suffixes in TAT protocols according to sex.**

|       | <i>-ing</i> > <i>-in</i> | <i>-ing</i> < <i>-in</i> |
|-------|--------------------------|--------------------------|
| Boys  | 5                        | 7                        |
| Girls | 10                       | 2                        |

Chi square: 2.84;  $0.05 < P < .1$  (by two-tailed test)

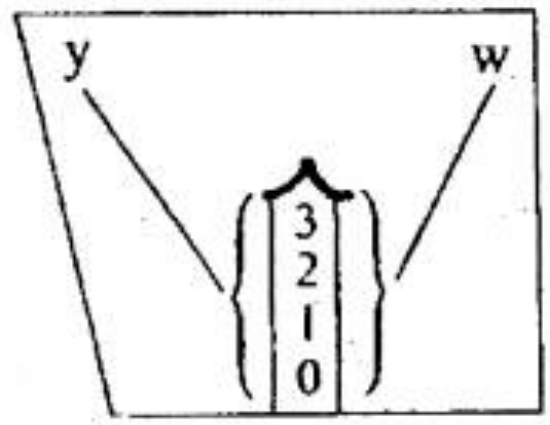
Fischer, John L. 1958. Social influences on the choice of a linguistic variant. *Word* 14(1): 47-56.

|   | Scale I           |       | Scale II |
|---|-------------------|-------|----------|
| 1 | [a]               | ————— | 0        |
| 2 | [a <sup>+</sup> ] | ————— | 1        |
| 3 | [a <sup>+</sup> ] | ————— |          |
| 4 | [a]               | ————— | 2        |
| 5 | [a <sup>+</sup> ] | ————— |          |
| 6 | [e]               | ————— | 3        |

(ay)

wife  
night  
right  
I

Close



(aw)

house  
out  
about  
mouth

Open

TABLE 3. GEOGRAPHICAL DISTRIBUTION OF CENTRALIZATION

|                | CI /ai/ | CI /au/ | CI /ai/ | CI /au/ |
|----------------|---------|---------|---------|---------|
| Down-island    |         |         | 0.35    | 0.33    |
| Edgartown      | 0.48    | 0.55    |         |         |
| Oak Bluffs     | 0.33    | 0.10    |         |         |
| Vineyard Haven | 0.24    | 0.33    |         |         |
| Up-island      |         |         | 0.61    | 0.66    |
| Oak Bluffs     | 0.71    | 0.99    |         |         |
| No. Tisbury    | 0.35    | 0.13    |         |         |
| West Tisbury   | 0.51    | 0.51    |         |         |
| Chilmark       | 1.00    | 0.81    |         |         |
| Gay Head       | 0.51    | 0.81    |         |         |

TABLE 4. CENTRALIZATION BY OCCUPATIONAL GROUPS

|           | CI /ai/ | CI /au/ |
|-----------|---------|---------|
| fishermen | 1.00    | 0.79    |
| farmers   | 0.32    | 0.22    |
| others    | 0.41    | 0.57    |

TABLE 5. CENTRALIZATION BY ETHNIC GROUPS

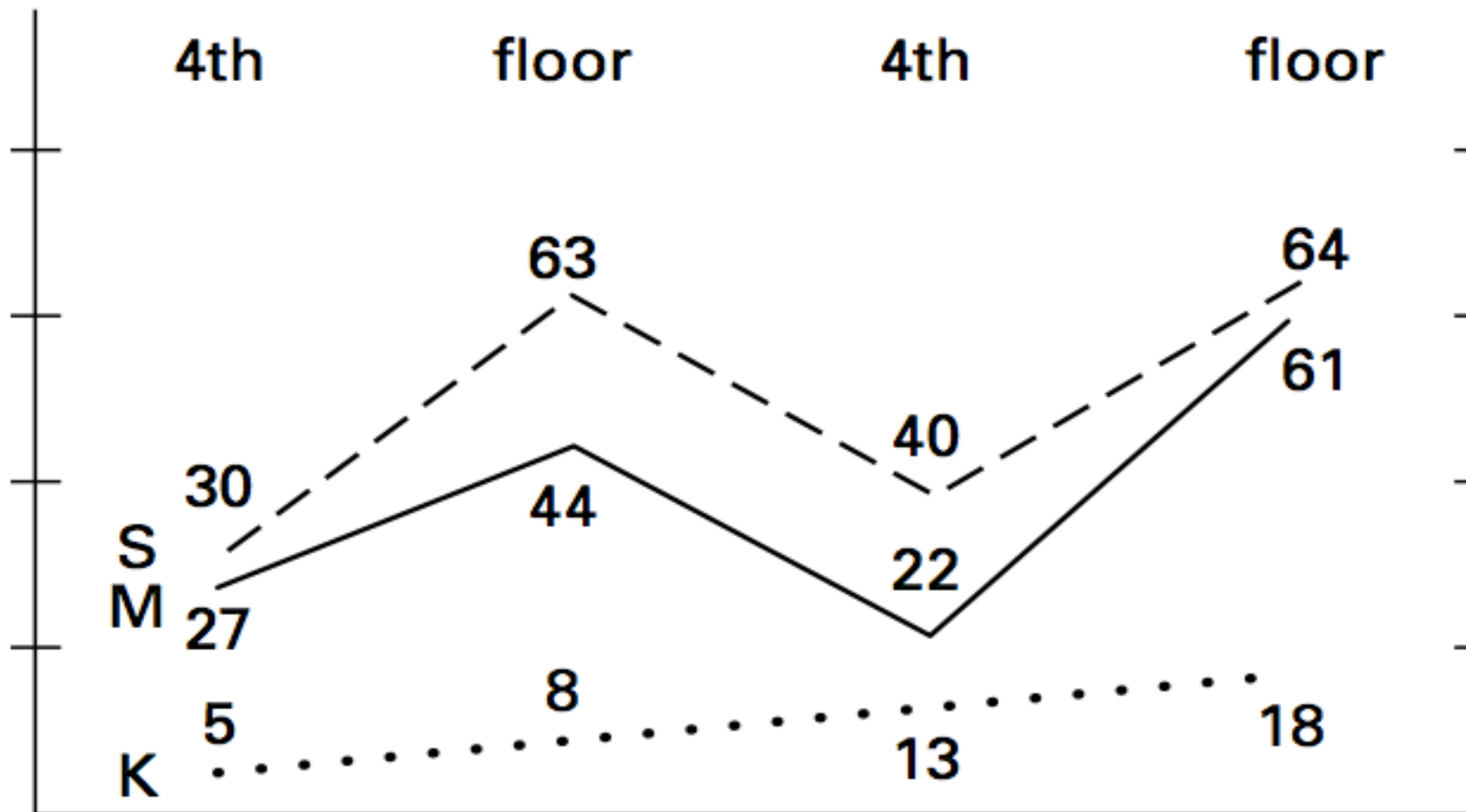
| <i>Age Level</i> | English |      | Portuguese |      | Indian |      |
|------------------|---------|------|------------|------|--------|------|
|                  | CI      | CI   | CI         | CI   | CI     | CI   |
|                  | /ai/    | /au/ | /ai/       | /au/ | /ai/   | /au/ |
| over 60          | 0.36    | 0.34 | 0.26       | 0.26 | 0.32   | 0.40 |
| 46 to 60         | 0.85    | 0.63 | 0.37       | 0.59 | 0.71   | 1.00 |
| 31 to 45         | 1.08    | 1.09 | 0.73       | 0.83 | 0.80   | 1.33 |
| under 30         | 0.35    | 0.31 | 0.34       | 0.52 | 0.47   | 0.88 |
| all ages         | 0.67    | 0.60 | 0.42       | 0.54 | 0.56   | 0.90 |

TABLE 6. CENTRALIZATION AND ORIENTATION TOWARDS MARTHA'S VINEYARD

| <i>Persons</i> |          | CI /ai/ | CI /au/ |
|----------------|----------|---------|---------|
| 40             | Positive | 0.63    | 0.62    |
| 19             | Neutral  | 0.32    | 0.42    |
| 6              | Negative | 0.09    | 0.08    |

The fact that this table shows us the sharpest example of stratification we have yet seen, indicates that we have come reasonably close to a valid explanation of the social distribution of centralized diphthongs.

Labov, William. 1963. The social motivation of a sound change. *Word* 19: 273-309.



(S=Saks, M=Macy's, K=S. Klein)

Figure 3.2 Percentage of *all (r-1)* by store for four positions

Labov, William. 1966. *The social stratification of English in New York City*. Ph.D. dissertation, Columbia.

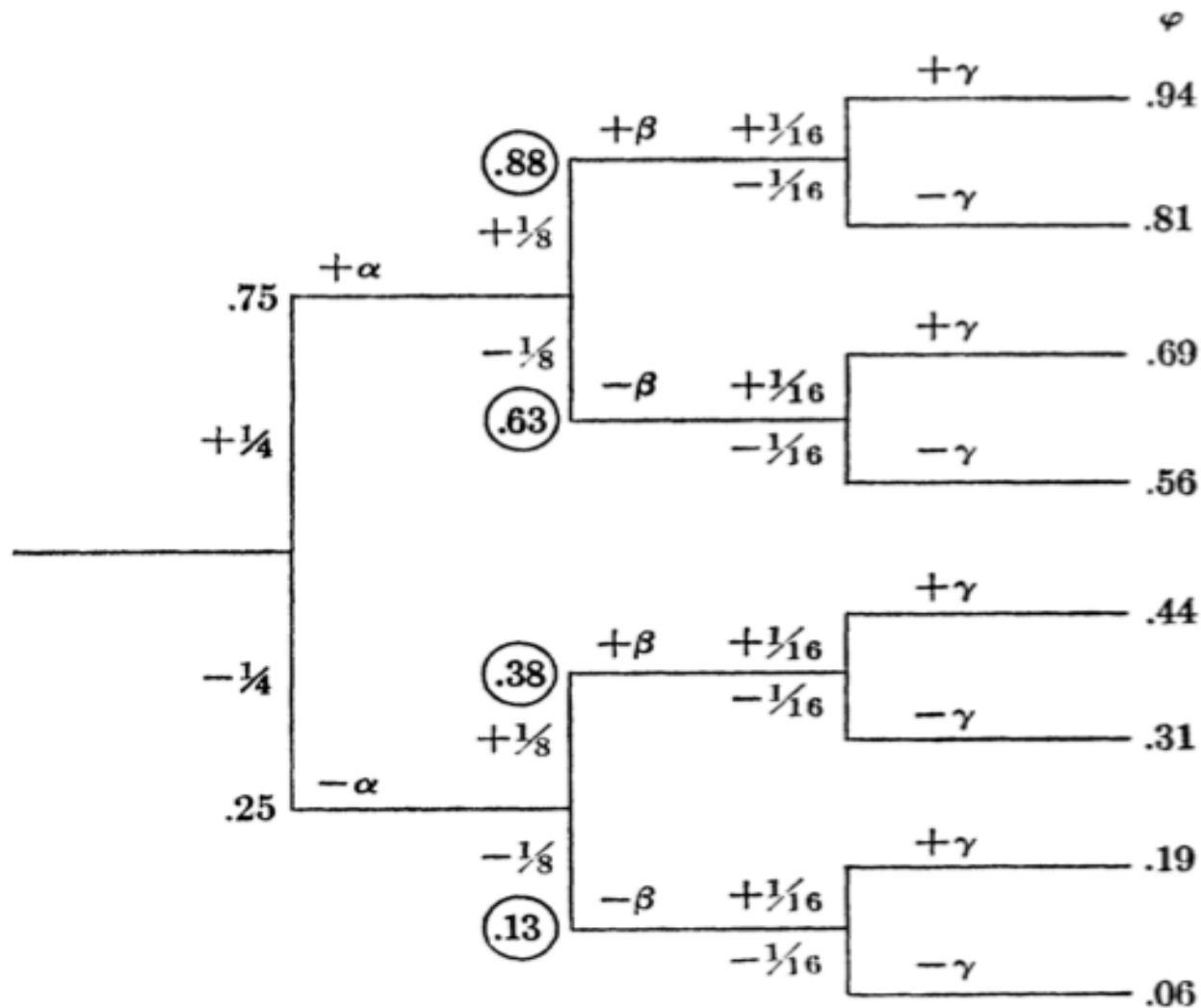


FIGURE 10  
Geometric ordering of variable constraints  $\alpha$ ,  $\beta$ ,  $\gamma$ .

Labov, William. 1969. Contraction, deletion, and inherent variability of the English copula. *Language*.



Input probability  $p_0 = 1$ .

|                        |         |  |         |
|------------------------|---------|--|---------|
| Preceding environment: | [+sib]— | $\begin{bmatrix} +cns \\ -sib \end{bmatrix}$ — | [−cns]— |
| Effect:                | 1       | 0.85   | 0.37    |
| Following environment: | —[+sib] | $\begin{bmatrix} +cns \\ -sib \end{bmatrix}$   | —[−cns] |
| Effect:                | 1       | 0.50   | 0.10    |
| Occupational class:    | workers | professional                                   |         |
| Effect:                | 1       | 0.35   |         |
| Sex:                   | women   | men  |         |
| Effect:                | 1       | 1  |         |

TABLE 6. Effect of each factor affecting *que* deletion in MF, according to a multiplicative application probabilities model.

Cedergren, Henrietta & Sankoff, David. 1974. Variable rules: performance as a statistical reflection of competence. *Language*.

$$p = \beta_0 + \beta_a + \dots + \beta_n$$

$$p = p_0 + p_i + p_j + \dots + p_k$$

$$\log p = \beta_0 + \beta_a + \dots + \beta_n$$

$$p = p_0 \times p_i \times p_j \times \dots \times p_k$$

$$\log \frac{p}{1-p} = \beta_0 + \beta_a + \dots + \beta_n$$

$$\left( \frac{p}{1-p} \right) = \left( \frac{p_0}{1-p_0} \right) \times \left( \frac{p_i}{1-p_i} \right) \times \left( \frac{p_j}{1-p_j} \right) \times \dots \times \left( \frac{p_k}{1-p_k} \right)$$

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TABLE 3.2

*Contribution of Grammatical Category, Following Phonological Segment, and Following Stress to the Deletion of Plural (s)<sup>a</sup>*

| Grammatical category |     | Following phonological segment |     | Following stress |     |
|----------------------|-----|--------------------------------|-----|------------------|-----|
| Adjective            | .69 | Pause                          | .65 | Weak             | .56 |
| Noun                 | .57 | Consonant                      | .47 | Heavy            | .44 |
| Determiner           | .26 | Vowel                          | .37 |                  |     |

<sup>a</sup> Input probability = .65.

Poplack, Shana. 1980. The notion of the plural in Puerto Rican Spanish: competing constraints on (s) deletion. In Labov (ed.)

$$\left(\frac{p}{1-p}\right) = \left(\frac{p_0}{1-p_0}\right) \times \left(\frac{p_i}{1-p_i}\right) \times \left(\frac{p_j}{1-p_j}\right) \times \dots \times \left(\frac{p_k}{1-p_k}\right)$$

TABLE 6. *Social factors contributing to the Canadian Vowel Shift in younger Toronto English speakers, by ethnic group and EO status (excluding tokens preceding a nasal consonant)*

|                                |         | (e)        | (æ)        |
|--------------------------------|---------|------------|------------|
| Total N:                       |         | 2,270      | 1,404      |
| Input:                         |         | .205       | .201       |
| <b>Ethnicity and EO Status</b> |         |            |            |
| British/Irish                  |         | <b>.68</b> | .51        |
| Italian                        | Low EO  | .54        | <b>.60</b> |
|                                | High EO | <b>.63</b> | <b>.82</b> |
| Chinese                        | Low EO  | .32        | .29        |
|                                | High EO | .30        | .17        |
| <i>Range:</i>                  |         |            | 38         |
| <b>Speaker Sex</b>             |         |            | 65         |
| Women                          |         | <b>.56</b> | <b>.60</b> |
| Men                            |         | .44        | .42        |
| <i>Range:</i>                  |         |            | 8          |
|                                |         |            | 18         |

Hoffman, Michol F. & Walker, James A. 2010. Ethnolects and the city: ethnic orientation and linguistic variation in Toronto English. *Language Variation and Change* 22: 37-67.

$$\left(\frac{p}{1-p}\right) = \left(\frac{p_0}{1-p_0}\right) \times \left(\frac{p_i}{1-p_i}\right) \times \left(\frac{p_j}{1-p_j}\right) \times \dots \times \left(\frac{p_k}{1-p_k}\right)$$

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| <i>Range:</i>                  |         |            | 38         |
|                                |         |            | 65         |
| <b>Speaker Sex</b>             |         |            |            |
| Women                          |         | <b>.56</b> | <b>.60</b> |
| Men                            |         | .44        | .42        |
| <i>Range:</i>                  |         |            | 8          |
|                                |         |            | 18         |

Each token was coded impressionistically as shifted or nonshifted, excluding any tokens where agreement between the authors could not be reached.

EO (ethnic orientation): For example, informants who identified themselves as “Canadian” received a score of 1; those who responded “Italian” received a score of 3; a response of “Italian-Canadian” or “both” received a score of 2.

# response and predictors: categorical or continuous

categorical (binary) response  
logistic regression

continuous response  
linear regression

categorical  
predictors

GoldVarb  
factor weights  
or log-odds  
coefficients

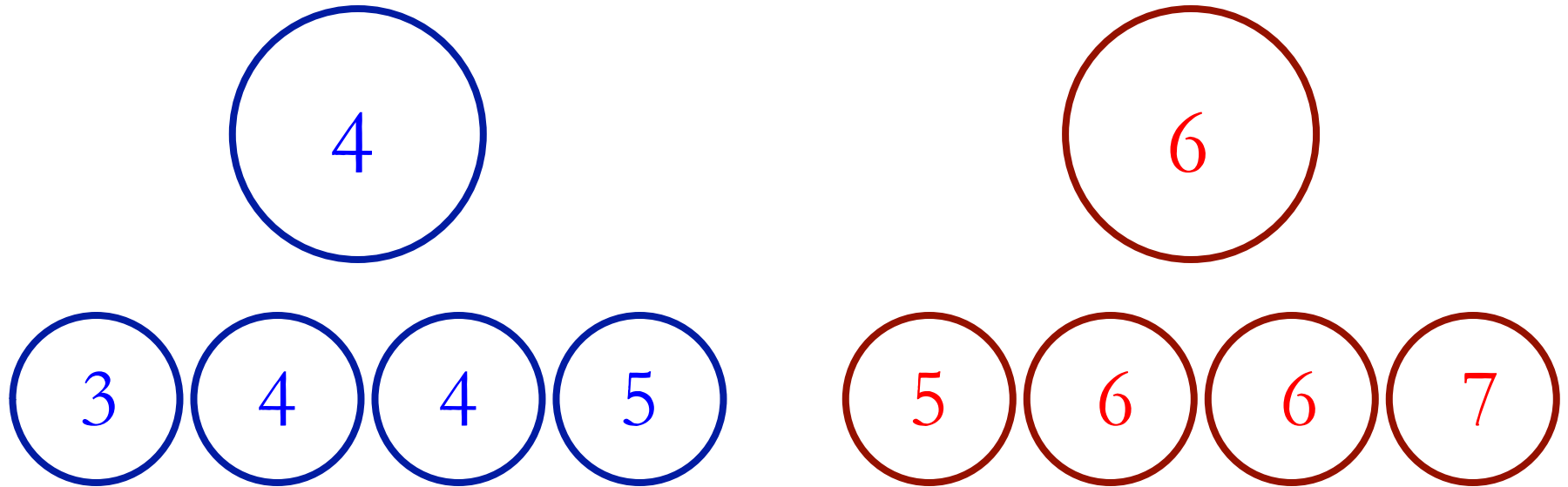
no GoldVarb  
no factor weights  
coefficients in same  
units as response

continuous  
predictors

no GoldVarb  
log-odds  
coefficients

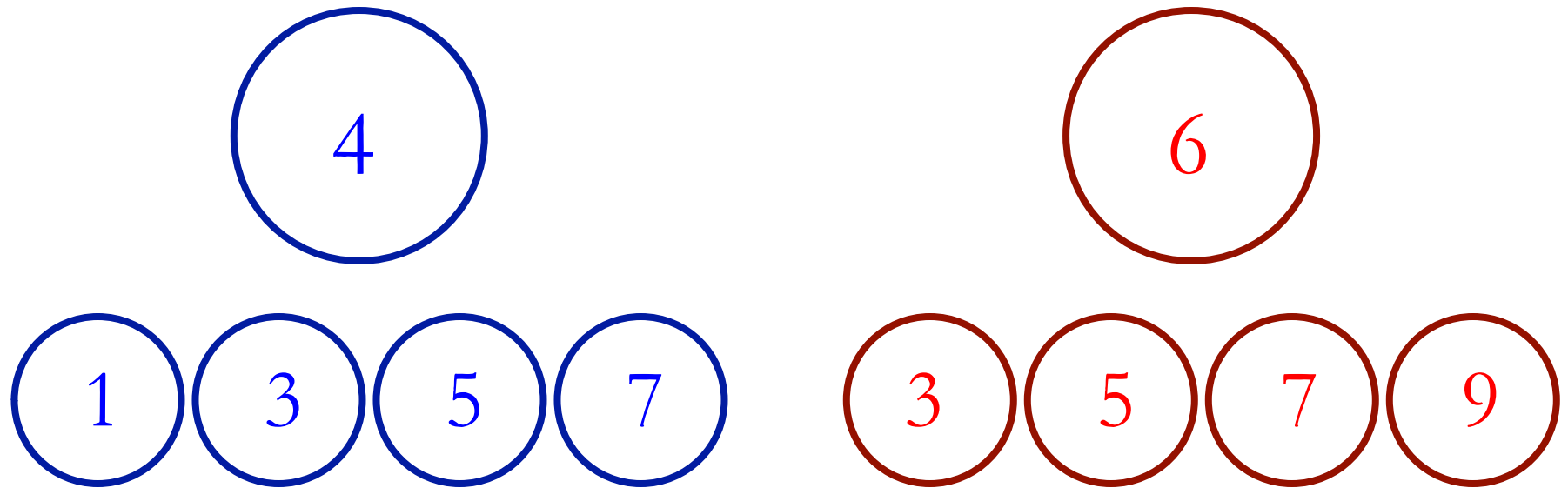
no GoldVarb  
no factor weights  
coefficients in same  
units as response

within-group differences affect the  
significance of between-group differences



small within-group variation  
significant between-group difference

within-group differences affect the significance of between-group differences



large within-group variation  
non-significant between-group difference



```
> age.fixed <- glm(tq1 ~ Age, buck, family = binomial)
> summary(age.fixed)
```

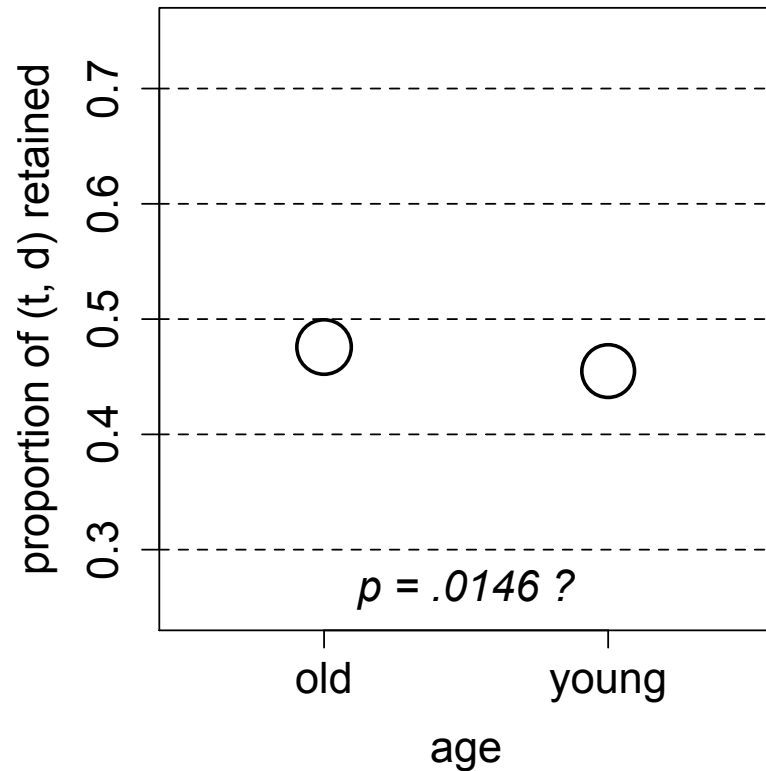
Coefficients:

|             | Estimate | Std. Error | z value | Pr(> z )    |
|-------------|----------|------------|---------|-------------|
| (Intercept) | -0.09701 | 0.02384    | -4.070  | 4.7e-05 *** |
| Ageyoung    | -0.08386 | 0.03433    | -2.443  | 0.0146 *    |

ONE-LEVEL ANALYSIS OF RESPONSE tq1 WITH PREDICTOR(S):  
Age (0.0146)

\$Age

| factor | logodds | tokens | 1/1+0 | centered | factor | weight |
|--------|---------|--------|-------|----------|--------|--------|
| old    | 0.042   | 7056   | 0.476 |          |        | 0.51   |
| young  | -0.042  | 6608   | 0.455 |          |        | 0.49   |



```
> age.mixed <- glmer(tq1 ~ Age + (1 | Speaker), buck,
family = binomial)
> summary(age.mixed)
```

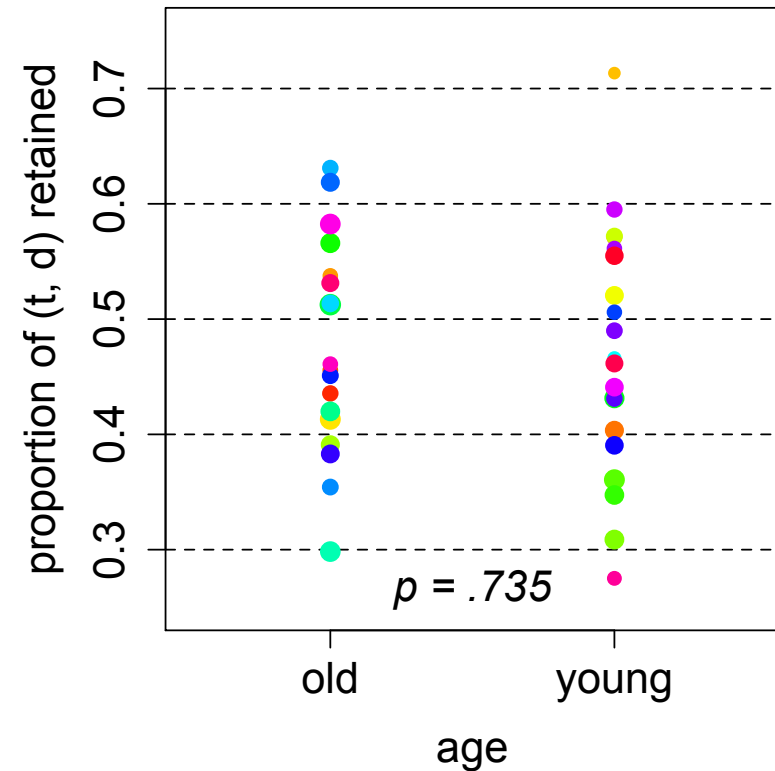
Fixed effects:

|             | Estimate | Std. Error | z value | Pr(> z ) |
|-------------|----------|------------|---------|----------|
| (Intercept) | -0.08842 | 0.08805    | -1.004  | 0.315    |
| Ageyoung    | -0.04229 | 0.12471    | -0.339  | 0.735    |

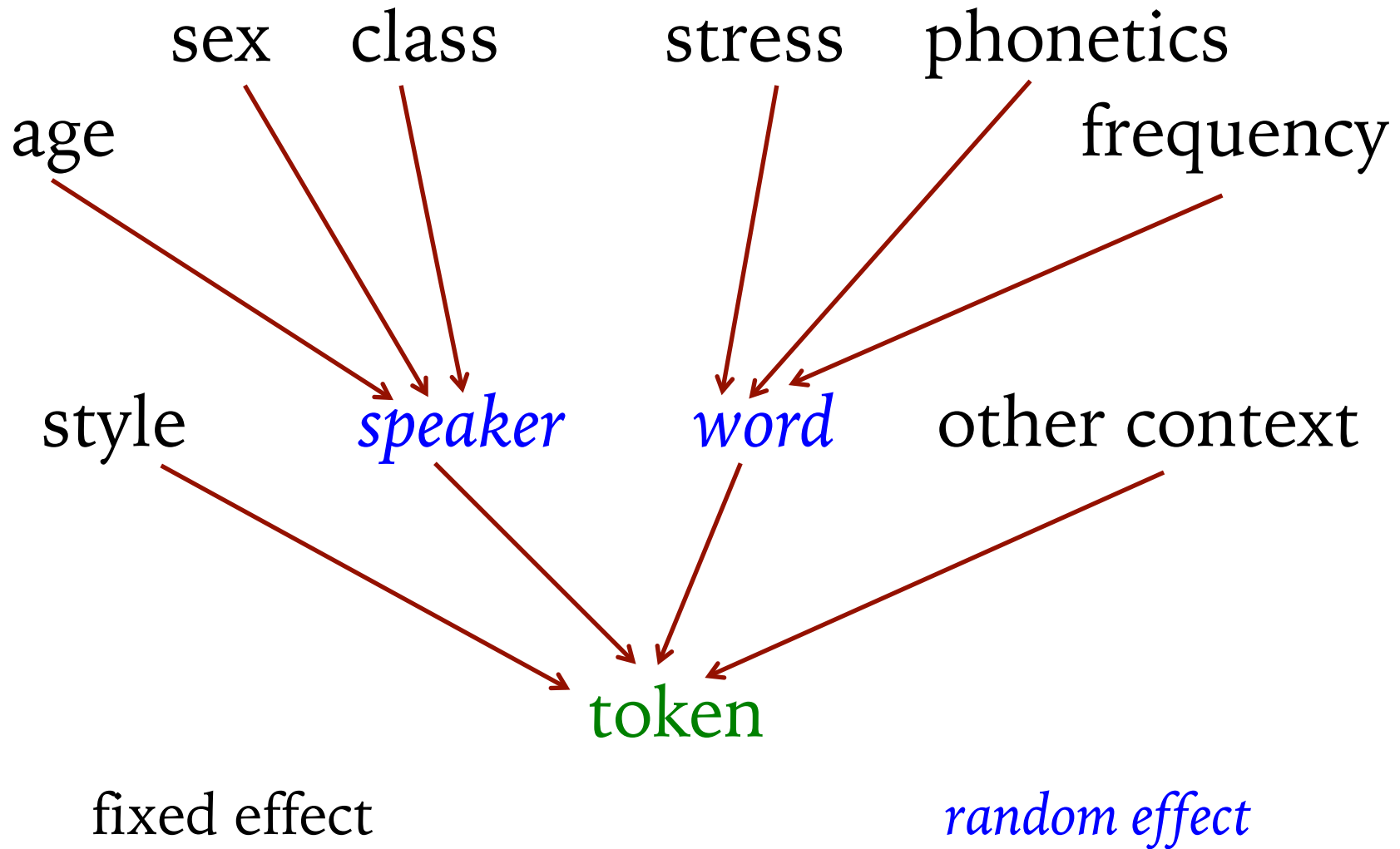
ONE-LEVEL ANALYSIS OF RESPONSE tq1 WITH PREDICTOR(S):  
Speaker [random, not tested] and Age (0.735)

\$Age

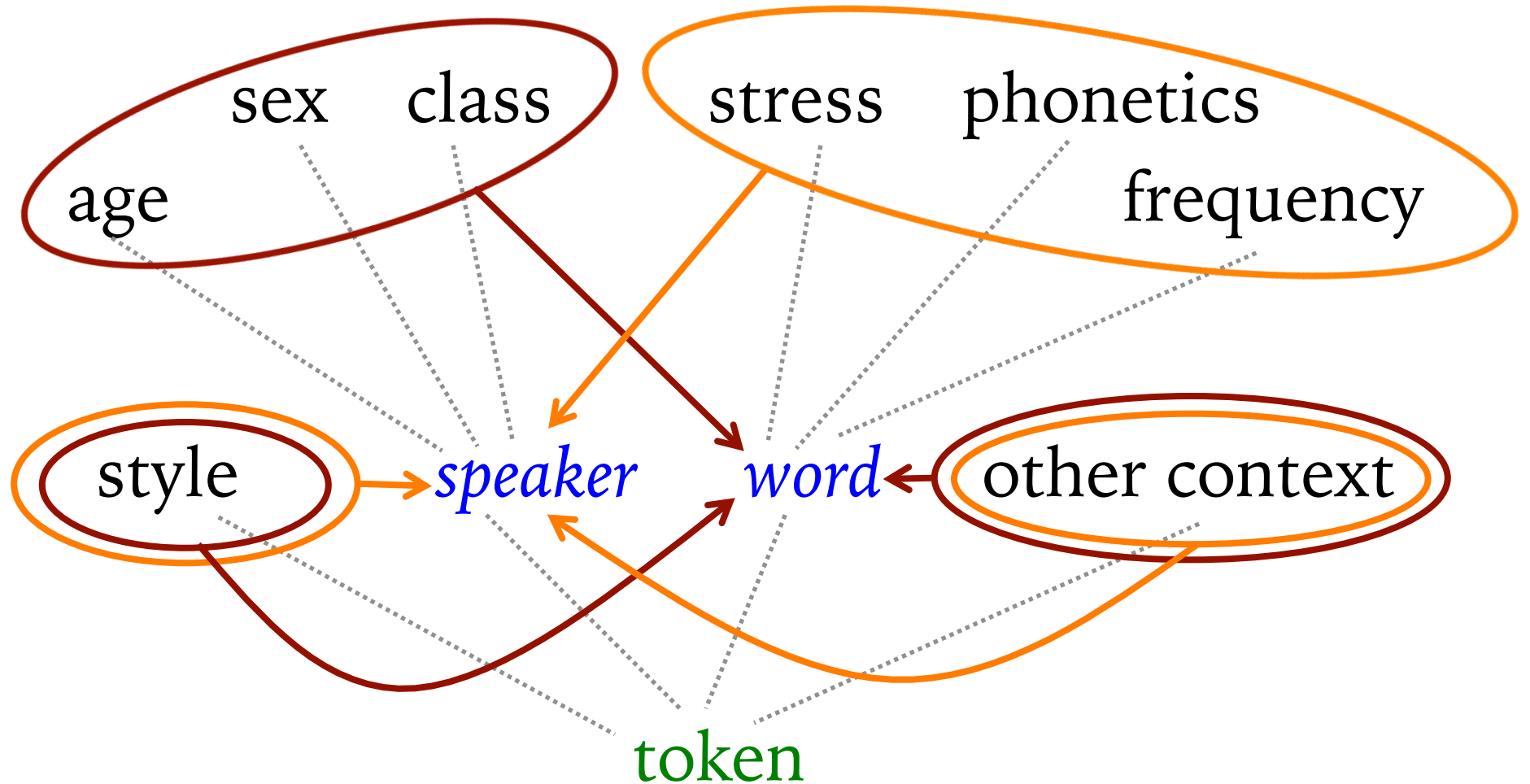
| factor | logodds | tokens | 1/1+0 | centered | factor | weight |
|--------|---------|--------|-------|----------|--------|--------|
| old    | 0.021   | 7056   | 0.476 |          |        | 0.505  |
| young  | -0.021  | 6608   | 0.455 |          |        | 0.495  |



# nesting: the relationship of variables in the mixed-effects model



# random intercepts and random slopes



*random intercept*

*random slope (by speaker)*

*random slope (by word)*

# individual-speaker variation: are mixed models necessary?

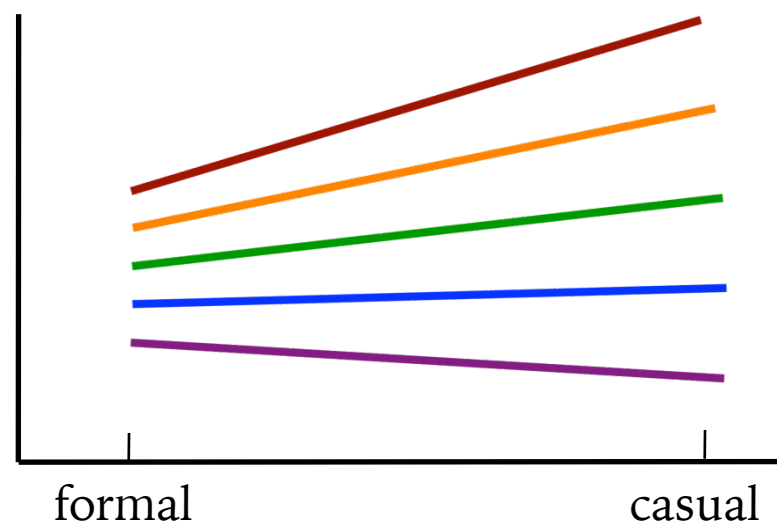
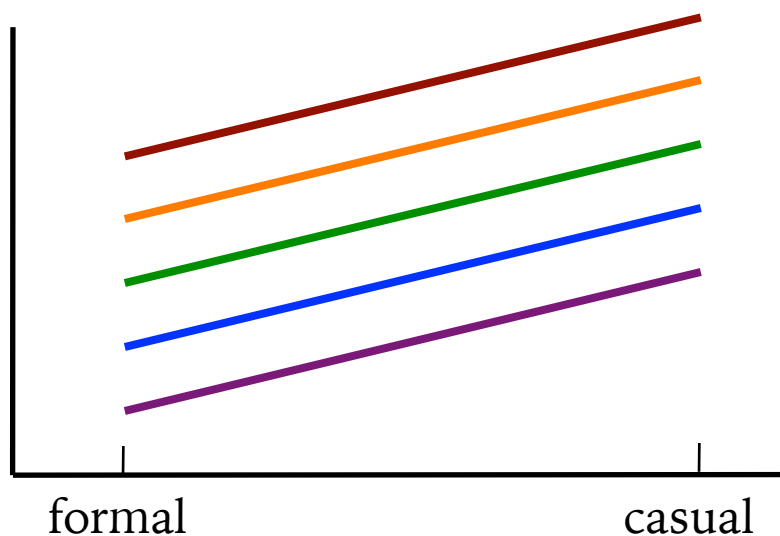
if only one speaker: *no!*

if no repeated measures per speaker: *no! (dep't stores)*

if every by-speaker difference is accounted for: *no!*

if they differ in overall rate/use of variable? *intercept!*

if they differ in the effect of other predictors? *slope(s)!*



# individual-word variation: are mixed models necessary?

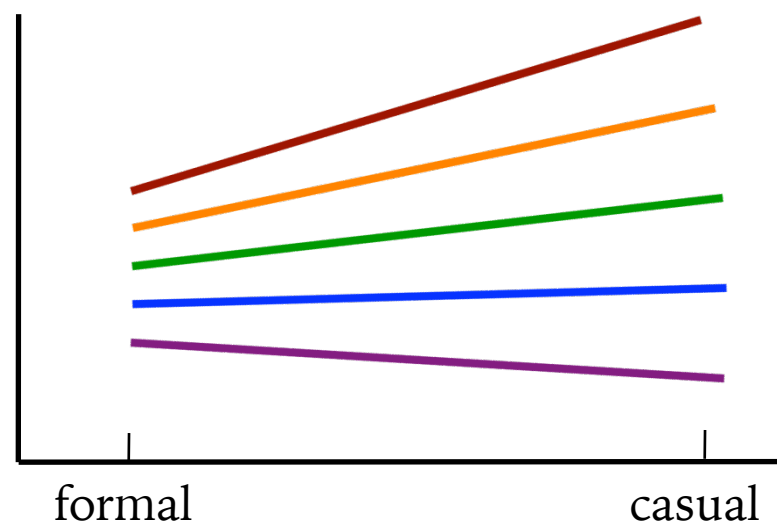
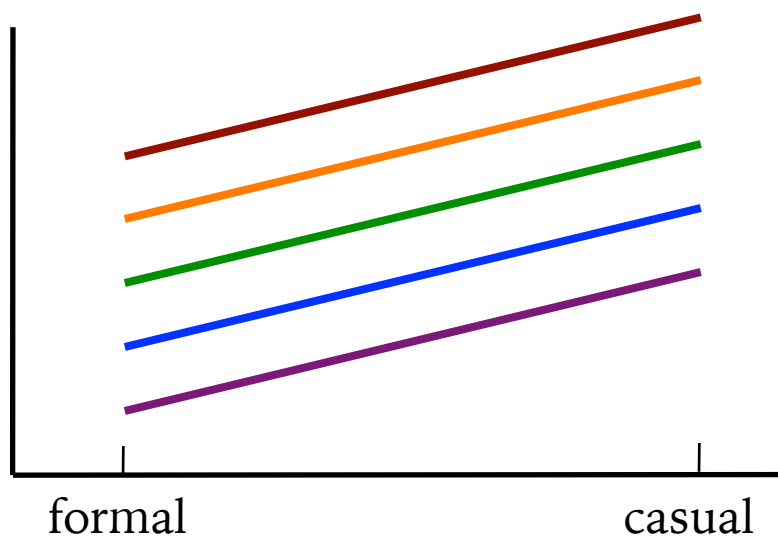
if only one word: *no!*

if no repeated measures per word: *no!* (*dep't stores*)

if every by-word difference is accounted for: *no!*

if words differ in overall rate/use of variable? *intercept!*

if words differ in effect of other predictor(s)? *slope(s)!*



# individual-speaker and -word variation: the received wisdom

do speakers differ in overall rate/use of variable?

- acknowledged to be true
- ignored in statistical practice

do speakers differ in the effect of other predictor(s)?

- claimed to be false (within a speech community)
- possibly true, ignored in statistical practice

do words differ overall *or* in the effect of predictor(s)?

- may depend on phon. theory, ignored in practice

is regression enough?

how am I going to do this?

what is R?

what is Rbrul?

what about RStudio?

are there any good books?

who else can I ask for help with statistics?

# starting with R and Rbrul

- 1) To download and install R, go to: <http://cran.r-project.org>
- 2) To install “packages” that will be needed, start R and execute these commands by typing at the > prompt:
  - > `install.packages(“ggplot2”)` (this is one graphics package)
  - > `install.packages(“lme4”)` (this is for mixed models)
  - > `install.packages(“lmerTest”)` (this helps lme4 provide p-values)If these install cleanly, you will not need to install them again.
- 3) To load packages (needs to be done each time you start R):
  - > `load(ggplot2)`      > `load(lme4)`      > `load(lmerTest)`
- 4) To install Rbrul (needs to be done each time you start R):
  - > `source(“http://www.danielezrajohnson.com/Rbrul.R”)`
- 5) To start Rbrul:
  - > `rbrul()`